

# ICRAMCS 2026

THE EIGHTH EDITION OF THE INTERNATIONAL CONFERENCE ON  
RESEARCH IN APPLIED MATHEMATICS AND COMPUTER SCIENCE  
April 23-24-25, 2026 | Marrakech, Morocco



## On the asymptotic behavior of solutions of inhomogeneous boundary transport processes

### Communication Info

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#### Keywords:

- (1) Inhomogeneous boundary evolution equations
- (2) network flow
- (3) (Asymptotically) almost periodic

### Abstract

This work investigates the solution's behavior for a class of transport processes on networks, characterized by space-dependent velocities and edge absorption, coupled with inhomogeneous vertex Kirchhoff's conditions. The problem is reformulated within the framework of inhomogeneous boundary evolution equations, allowing a variation of constants formula expressing the mild solution. Assuming asymptotically almost periodic (AAP) exogenous terms on Banach space and on a boundary space respectively, we prove that every bounded solution on half-line is likewise AAP. Moreover, we identify conditions on the initial data that yield AAP behavior. These theoretical results are applied to the network model, ensuring the existence and uniqueness of AAP solutions. Finally, we illustrate our findings with numerical simulations, confirming their practical applicability. Our approach combines tools from semi-group theory, Greiner's method, spectral theory, numerical analysis...

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