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## Optimal Control Approach for Bilateral Elastic Contact Problem with Power-Law

### Communication Info

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(2) multivalued equation

(3) Clarke subdifferential

### Abstract

This paper develops a variational optimal control framework to analyze a bilateral elastic contact problem with power-law friction, where non-penetration conditions and nonlinear friction are modeled via the Clarke subdifferential of a nonsmooth potential energy functional, following the hemivariational inequality theory of [1,2]. Reformulating the problem as a nonlinear multivalued inclusion  $f \in Fy + \partial\Phi(y)$  in a Hilbert space, we establish the existence and uniqueness of a weak solution using abstract results from dynamic inclusion theory, extending techniques for elliptic variational inequalities [3]. The optimal control approach—inspired by energy-based schemes in [4]—minimizes a global functional, reducing high-order PDEs to tractable lower-order systems while enhancing solution regularity, a critical step for numerical implementation. The model generalizes classical Coulomb friction via power-law regularization, a technique validated for granular materials and soft tissues, broadening applicability to industrial processes like metal forming or biomechanics. By bridging variational analysis, contact mechanics, and control theory, this work advances theoretical and computational tools for complex contact problems, offering a flexible foundation for future simulations in solid mechanics.

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